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# The Lorenz95 system

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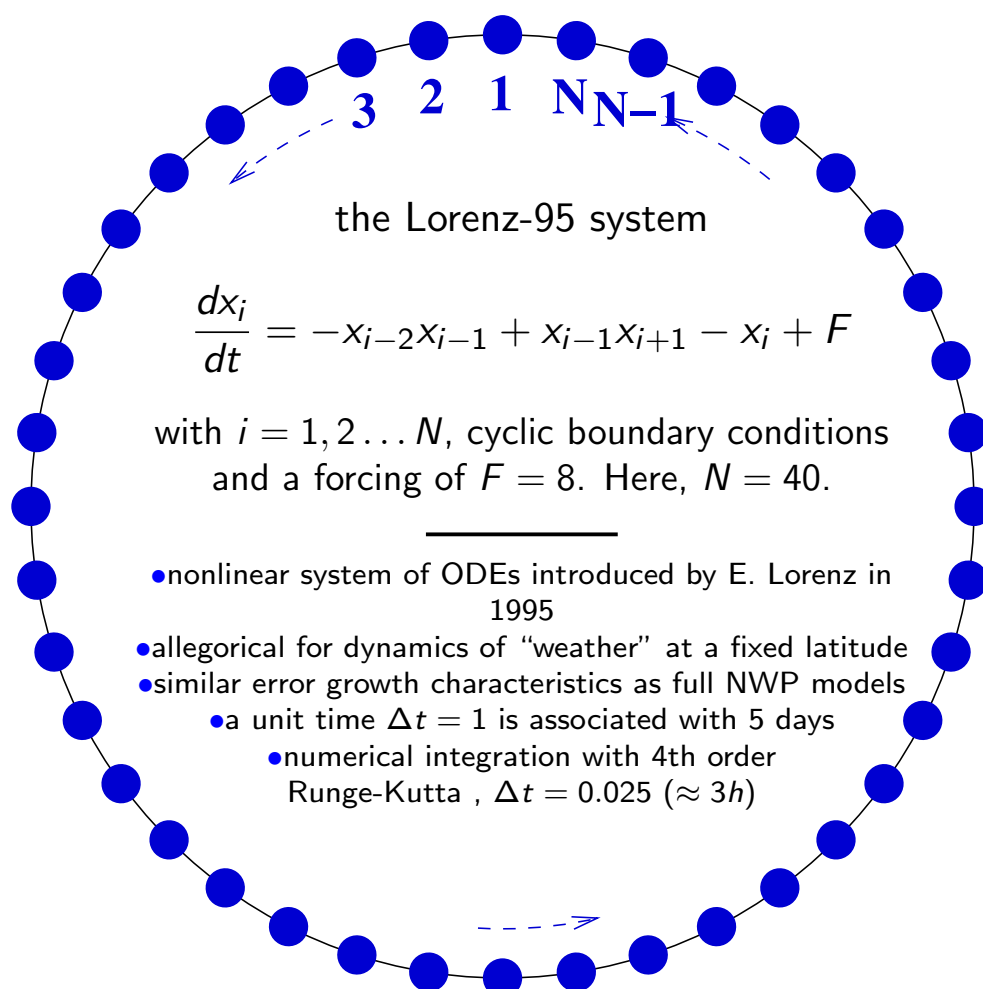
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## Acknowledgment

*Some parts of the L95 introduction and the integration part of the scilab programs have been taken from the ECMWF data-assimilation tutorial by Martin Leutbecher*

# Introduction

- The L95 system is a simple dynamical system that exhibits chaotic dynamics in a spatially extended domain.
- Appears frequently in publications on data assimilation methods where an idealized setting is desired.
- It could help you to understand, repeat and extend some of the published studies.
- The system is small enough to run an Ensemble Kalman Filter for many assimilation cycles on a personal computer. Yet, it is not too small to be completely trivial.



## L95 system

- With the forcing used here,  $F = 8$ , the system behaves chaotic:

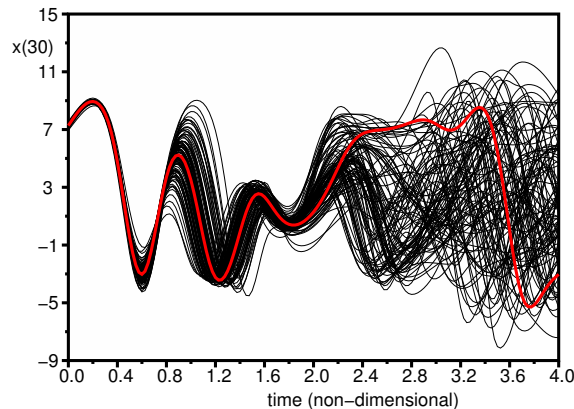


Fig. 1: gridpoint 30 as a function of time for slightly different initial conditions

- With this settings the system has 13 positive Lyapunov exponents, the largest one corresponds to a doubling time of 2.1 days.
- Variables fluctuate about the mean with a climatological standard deviation of  $\sigma_{clim} \approx 3.6$

## L95 system

- The dynamic is the same for each variable; the equation is invariant under a transformation  $i \rightarrow i + 1$ .
- A perturbation of the initial condition will grow and its leading edge propagates “eastward” (higher indices) at a speed of about 25 degrees/day - corresponding to 14 indices in a (non-dimensional) time unit.
- Due to these properties the L95 system can be used as a toy model for data assimilation; it has some of the features of realistic NWP systems but is low-dimensional
- limits of L95 system: e.g. *convective scale*; here, more sophisticated toy models are needed (e.g. *shallow water* models)

## References

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